#### Real Time Operating Systems and Middleware

#### **Real-Time Scheduling**

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#### **Definitions**

Algorithm  $\rightarrow$  logical procedure used to solve a problem

- Program → formal description of an algorithm, using a programming language
- Process  $\rightarrow$  instance of a program (program in execution)
  - Program: static entity
  - Process: dynamic entity
- The term task is used to indicate a schedulable entity (either a process or a thread)
  - ${\scriptstyle \bullet} \ \ \, \text{Thread} \rightarrow \text{flow of execution}$
  - Process  $\rightarrow$  flow of execution + private resources (address space, file table, etc...)

# Scheduling

- Tasks do not run on bare hardware...
  - The OS kernel creates the illusion of virtual CPU
  - One virtual CPU per task
  - Tasks have the illusion of executing concurrently
- Concurrency is implemented by multiplexing tasks on the same CPU...
  - Tasks are alternated on a real CPU...
  - ...And the task scheduler decides which task executes at a given instant in time
- Tasks are associated temporal constraints (deadlines)
  - The scheduler must allocate the CPU to tasks so that their deadlines are respected

#### Scheduler - 1

- The scheduler is responsible for generating a schedule starting from a set of tasks ready to execute
- Mathematical model
  - Let's start considering an UP system
    - A schedule  $\sigma(t)$  is a function mapping time t into an executing task

$$\sigma: t \to \mathcal{T} \cup \tau_{idle}$$

where  $\mathcal{T}$  is the set of tasks running in the system

- $\tau_{idle}$  is the *idle task*: when it is scheduled, the CPU becomes idle
- For an SMP system (*m* CPUs),  $\sigma(t)$  can be extended to map *t* in vectors  $\tau \in (\mathcal{T} \cup \tau_{idle})^m$

#### Scheduler - 2

- The scheduler is responsible for selecting the task to execute
- From an algorithmic point of view
  - Scheduling algorithm → Algorithm used to select for each time instant t a task to be executed on a CPU among the ready task
  - Given a task set T, a scheduling algorithm A generates the schedule  $\sigma_A(t)$
- A task set is schedulable by an algorithm A if  $\sigma_A$  does not contain missed deadlines
- Schedulability test  $\rightarrow$  check if  $\mathcal{T}$  is schedulable by  $\mathcal{A}$

# **RT Scheduling: Why?**

• The task set  $\mathcal{T} = \{(1,3), (4,8)\}$  is not schedulable by FCFS



•  $\mathcal{T} = \{(1,3), (4,8)\}$  is schedulable with other algorithms



## **RT Scheduling Anomalies**

• Consider jobs  $J_{1,1}$  and  $J_{1,2}$  using a semaphore...

• 
$$r_{1,1} = 2$$
,  $c_{1,1} = 6$ ,  $d_{1,1} = 9$ 

• 
$$r_{2,1} = 0$$
,  $c_{2,1} = 12$ ,  $d_{2,1} = 24$ 



**•** Faster processor ( $c_{1,1} = 4.5$ ,  $c_{2,1} = 9$ )



# **Cyclic Executive Scheduling**

- Very popular in military and avionics systems
- Also called timeline scheduling or cyclic scheduling
- Originally used for periodic tasks
- Examples:
  - Air traffic control
  - Space Shuttle
  - Boeing 777

#### The idea

- Static scheduling algorithm
- Jobs are not preemptable
  - A scheduled job executes until termination
- The time axis is divided in time slots
- Slots are statically allocated to the tasks (scheduling table)
- A periodic timer activates execution (allocation of a slot)
  - Major Cycle: least common multiple (lcm) of all the tasks' periods (also called *hyperperiod*)
  - Minor Cycle: greatest common divisor (gcd) of all the tasks' periods
  - $\checkmark$  A timer fires every Minor Cycle  $\Delta$

## Example



#### Implementation



## Advantages

- Simple implementation (no real-time operating system is required)
  - No real task exist: just function calls
    - One single stack for all the "tasks"
- Non-preemptable scheduling  $\Rightarrow$  no need to protect data
  - No need for semaphores, pipes, mutexes, mailboxes, etc.
- Low run-time overhead
- Jitter can be explicitly controlled

#### **Drawbacks**

- Not robust during overloads
- Difficult to expand the schedule (static schedule)
  - New task ⇒ the whole schedule must be recomputed
- Not easy to handle aperiodic/sporadic tasks
- All task periods must be a multiple of the minor cycle time
- Difficult to incorporate processes with long periods (big tables)
- Variable computation time  $\Rightarrow$  it might be necessary to split tasks into a fixed number of fixed size procedures

## **Overload Management**

What do we do during task overruns?

- Let the task continue? ...
  - Possible domino effect on all the other tasks (timeline break)
- Abort the task?
  - The system can remain in inconsistent states
- $\blacksquare$   $\Rightarrow$  not well suited for soft tasks...

## Extensibility

If one or more tasks need to be upgraded, we may have to re-design the whole schedule again

**Example:** B is updated but  $C_A + C_B > \Delta$ 



#### Extensibility

• We have to split B into two subtasks  $(B_1, B_2)$  and recompute the schedule.



## **Fixed Priority Scheduling**

- Very simple *preemptive* scheduling algorithm
  - Every task  $\tau_i$  is assigned a fixed priority  $p_i$
  - The active task with the highest priority is scheduled
- Priorities are integer numbers: the higher the number, the higher the priority
  - In the research literature, sometimes authors use the opposite convention: the lowest the number, the highest the priority
- In the following we show some examples, considering periodic tasks, constant execution times, and deadlines equal to the period































## **Another Example (non-schedulable)**

• Consider the following task set:  $\tau_1 = (3, 6, 6)$ ,  $p_1 = 3$ ,  $\tau_2 = (2, 4, 8)$ ,  $p_2 = 2$ ,  $\tau_3 = (2, 12, 12)$ ,  $p_3 = 1$ 



In this case, task  $\tau_2$  misses its deadline!

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In this case, task  $\tau_2$  misses its deadline!

# **Notes about Priority Scheduling**

- Some considerations about the schedule shown before:
  - The response time of the task with the highest priority is minimum and equal to its WCET
  - The response time of the other tasks depends on the interference of the higher priority tasks
  - The priority assignment may influence the schedulability of a task set
    - Problem: how to assign tasks' priorities so that a task set is schedulable?
## **Priority assignment**

# **Priority assignment**

- Given a task set, how to assign priorities?
- There are two possible objectives:
  - Schedulability (i.e. find the priority assignment that makes all tasks schedulable)
  - Response time (i.e. find the priority assignment that minimise the response time of a subset of tasks)
- By now we consider the first objective only
- An optimal priority assignment Opt is such that:
  - If the task set is schedulable with another priority assignment, then it is schedulable with priority assignment Opt
  - If the task set is not schedulable with Opt, then it is not schedulable by any other assignment

# **Optimal Priority Assignment**

- Given a periodic task set T with all tasks having relative deadline  $D_i$  equal to the period  $T_i$  ( $\forall i, D_i = T_i$ ), and with all offsets equal to 0 ( $\forall i, r_{i,0} = 0$ ):
  - The best assignment is the Rate Monotonic (RM) assignment
  - $\ \ \, \bullet \ \ \, Shorter\ period \rightarrow higher\ priority$
- Given a periodic task set with deadline different from periods, and with all offsets equal to 0 ( $\forall i$ ,  $r_{i,0} = 0$ ):
  - The best assignment is the *Deadline Monotonic* assignment
  - Shorter relative deadline  $\rightarrow$  higher priority
- For sporadic tasks, the same rules are valid as for periodic tasks with offsets equal to 0





































#### **Presence of offsets**

- If instead we consider periodic tasks with offsets, then there is no optimal priority assignment
  - In other words,
    - If a task set  $T_1$  is schedulable by priority  $O_1$  and not schedulable by priority assignment  $O_2$ ,
    - It may exist another task set  $T_2$  that is schedulable by  $O_2$  and not schedulable by  $O_1$ .
  - For example,  $\mathcal{T}_2$  may be obtained from  $\mathcal{T}_1$  simply changing the offsets!
- Anyway, all offsets = 0 is the *Worst Case*  $\Rightarrow$  if  $\mathcal{T}$  is schedulable when  $\forall i, r_{i,0} = 0$  then all the task sets obtained from  $\mathcal{T}$  by changing offsets are schedulable
- **•** Example:  $\mathcal{T} = \{(3, 7, 10), (5, 6, 10)\}$

## **Example of non-optimality with offsets**



#### Changing the offset:



# **Example of non-optimality with offsets**





#### Changing the offset:



# **Scheduling Analysis**

# Analysis

- Given a task set, how can we guarantee if it is schedulable of not?
- The first possibility is to simulate the system to check that no deadline is missed;
- The execution time of every job is set equal to the WCET of the corresponding task;
  - Periodic tasks with no offsets  $\Rightarrow$  sufficient to simulate the schedule until the *hyperperiod* ( $H = lcm\{T_i\}$ ).
  - Offsets  $\phi_i = r_{i,0} \Rightarrow$  simulate until  $2H + \phi_{max}$ .
  - If tasks periods are prime numbers the hyperperiod can be very large!
- Note: RM  $\rightarrow$  hyperperiod; Cyclic Executive  $\rightarrow$  Major Cycle

Exercise: Compare the hyperperiods of this two task sets:

• 
$$T_1 = 8$$
,  $T_2 = 12$ ,  $T_3 = 24$ 

• 
$$T_1 = 7, T_2 = 12, T_3 = 25$$

In case of sporadic tasks, we can assume them to arrive at the highest possible rate, so we fall back to the case of periodic tasks with no offsets!

### **Utilisation Analysis**

- In many cases it is useful to have a very simple test to see if the task set is schedulable.
- A sufficient test is based on the Utilisation bound:
  - The *utilisation least upper bound* for scheduling algorithm  $\mathcal{A}$  is the smallest possible utilisation  $U_{lub}$  such that, for any task set  $\mathcal{T}$ , if the task set's utilisation U is not greater than  $U_{lub}$  ( $U \leq U_{lub}$ ), then the task set is schedulable by algorithm  $\mathcal{A}$

#### Utilisation

Each task uses the processor for a fraction of time

$$U_i = \frac{C_i}{T_i}$$

The total processor utilisation is

$$U = \sum_{i} \frac{C_i}{T_i}$$

This is a measure of the processor's load

## **Necessary Condition**

- If U > 1 the task set is surely not schedulable
- However, if U < 1 the task set may or may not be schedulable . . .
- If  $U < U_{lub}$ , the task set is schedulable!!!
  - "Gray Area" between  $U_{lub}$  and 1
  - We would like to have  $U_{lub}$  near to 1
  - $U_{lub} = 1$  would be optimal!!!

## **Least Upper Bound**



#### **Utilisation Bound for RM**

- We consider n periodic (or sporadic) tasks with relative deadline equal to periods.
- Priorities are assigned with Rate Monotonic;

• 
$$U_{lub} = n(2^{1/n} - 1)$$

- $U_{lub}$  is a decreasing function of n;
- For large *n*:  $U_{lub} \approx 0.69$

n	U <sub>lub</sub>	n	$U_{lub}$
2	0.828	7	0.728
3	0.779	8	0.724
4	0.756	9	0.720
5	0.743	10	0.717
6	0.734	11	

### **Schedulability Test**

Therefore the schedulability test consist in:

- Computing  $U = \sum_{i=1}^{n} \frac{C_i}{T_i}$
- if  $U \leq U_{lub}$ , the task set is schedulable
- if U > 1 the task set is not schedulable
- if  $U_{lub} < U \leq 1$ , the task set may or may not be schedulable

Task set T composed by 3 periodic tasks with  $U < U_{lub}$ : the system is schedulable.

$$\tau_1 = (2, 8), \tau_2 = (3, 12), \tau_3 = (4, 16);$$

$$U = 0.75 < U_{lub} = 0.77$$



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By increasing the computation time of task  $\tau_3$ , the system may still be schedulable

$$\tau_1 = (2, 8), \tau_2 = (3, 12), \tau_3 = (5, 16);$$

$$U = 0.81 > U_{lub} = 0.77$$



#### **Utilisation Bound for DM**

If relative deadlines are less than or equal to periods, instead of considering  $U = \sum_{i=1}^{n} \frac{C_i}{T_i}$ , we can consider:

$$U' = \sum_{i=1}^{n} \frac{C_i}{D_i}$$

• Then the test is the same as the one for RM (or DM), except that we must use U' instead of U.

• Idea: 
$$\tau = (C, D, T) \rightarrow \tau' = (C, D, D)$$

- au' is a "worst case" for au
- If  $\tau'$  can be guaranteed,  $\tau$  can be guaranteed too

#### Pessimism

- The bound is very pessimistic: most of the times, a task set with  $U > U_{lub}$  is schedulable by RM.
- A particular case is when tasks have periods that are harmonic:
  - A task set is *harmonic* if, for every two tasks  $\tau_i, \tau_j$ , either  $T_i$  is multiple of  $T_j$  or  $T_j$  is multiple of  $T_i$ .
- For a harmonic task set, the utilisation bound is  $U_{lub} = 1$
- In other words, Rate Monotonic is an optimal algorithm for harmonic task sets

#### **Example of Harmonic Task Set**

